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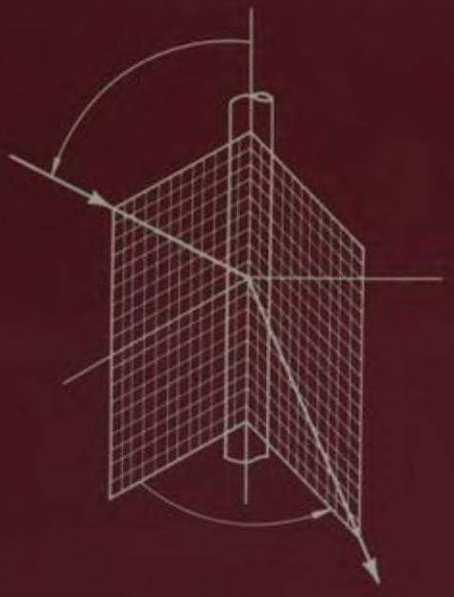
Absorption and Scattering of Light by Small Particles



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Absorption and Scattering of Light by Small Particles

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Contents

PART 1—BASIC THEORY

Chapter 1. Introduction, 3

1.1	Physical Basis for Scattering and Absorption	3
1.2	Scattering by Fluctuations and by Particles	4
1.3	Physics of Scattering by a Single Particle	7
1.4	Collections of Particles	9
1.5	The Direct and Inverse Problem	9
	Notes and Comments	11

Chapter 2. Electromagnetic Theory, 12

2.1	Field Vectors and the Maxwell Equations	12
2.2	Time-Harmonic Fields	14
2.3	Frequency-Dependent Phenomenological Coefficients	15
2.4	Spatial Dispersion	22
2.5	Poynting Vector	23
2.6	Plane-Wave Propagation in Unbounded Media	25
2.7	Reflection and Transmission at a Plane Boundary	30
2.8	Reflection and Transmission by a Slab	36
2.9	Experimental Determination of Optical Constants	41
2.10	The Analogy Between a Slab and a Particle	42
2.11	Polarization	44
	Notes and Comments	56

Chapter 3. Absorption and Scattering by an Arbitrary Particle, 57

3.1	General Formulation of the Problem	57
3.2	The Amplitude Scattering Matrix	61
3.3	Scattering Matrix	63
3.4	Extinction, Scattering, and Absorption	69
	Notes and Comments	81

Chapter 4. Absorption and Scattering by a Sphere, 82

4.1	Solutions to the Vector Wave Equations	83
4.2	Expansion of a Plane Wave in Vector Spherical Harmonics	89
4.3	The Internal and Scattered Fields	93
4.4	Cross Sections and Matrix Elements	101
4.5	Asymmetry Parameter and Radiation Pressure	119
4.6	Radar Backscattering Cross Section	120
4.7	Thermal Emission	123
4.8	Computation of Scattering Coefficients and Cross Sections	126
	Notes and Comments	129

Chapter 5. Particles Small Compared with the Wavelength, 130

5.1	Sphere Small Compared with the Wavelength	130
5.2	The Electrostatics Approximation	136
5.3	Ellipsoid in the Electrostatics Approximation	141
5.4	Coated Ellipsoid	148
5.5	The Polarizability Tensor	150
5.6	Anisotropic Sphere	152
5.7	Scattering Matrix	154

Chapter 6. Rayleigh–Gans Theory, 158

6.1	Amplitude Scattering Matrix Elements	158
6.2	Homogeneous Sphere	162
6.3	Finite Cylinder	163
	Notes and Comments	165

Chapter 7. Geometrical Optics, 166

7.1	Absorption and Scattering Cross Sections	166
7.2	Angular Distribution of the Scattered Light: Rainbow Angles	174
7.3	Scattering by Prisms: Ice Crystal Haloes	178
	Notes and Comments	180

Chapter 8. A Potpourri of Particles, 181

8.1	Coated Sphere	181
8.2	Anisotropic Sphere	184
8.3	Optically Active Particles	185
8.4	Infinite Right Circular Cylinder	194
8.5	Inhomogeneous Particles: Average Dielectric Function	213
8.6	A Survey of Nonspherical Particles, Regular and Irregular	219
	Notes and Comments	222

PART 2—OPTICAL PROPERTIES OF BULK MATTER

Chapter 9. Classical Theories of Optical Constants, 227

9.1	The Lorentz Model	228
9.2	The Multiple-Oscillator Model	244
9.3	The Anisotropic Oscillator Model	247
9.4	The Drude Model	251
9.5	The Debye Relaxation Model	259
9.6	General Relationship Between ϵ' and ϵ''	265
	Notes and Comments	267

Chapter 10. Measured Optical Properties, 268

10.1	Optical Properties of an Insulating Solid: MgO	268
10.2	Optical Properties of a Metal: Aluminum	271
10.3	Optical Properties of a Liquid: Water	273
10.4	A Comment on the Magnitude of k	279
10.5	Validity of Bulk Optical Constants in Small-Particle Calculations	280
10.6	Summary of Absorption Mechanism and Temperature Effects	281
	Notes and Comments	283

PART 3—OPTICAL PROPERTIES OF PARTICLES

Chapter 11. Extinction, 287

11.1	Extinction = Absorption + Scattering	287
11.2	Extinction Survey	289
11.3	Some Extinction Effects in Insulating Spheres	295
11.4	Ripple Structure	300
11.5	Absorption Effects in Extinction	305
11.6	Extinction Calculations for Nonspherical Particles	310
11.7	Extinction Measurements	316
11.8	Extinction: A Synopsis	323
	Notes and Comments	324

Chapter 12. Surface Modes in Small Particles, 325

12.1	Surface Modes in Small Spheres	326
12.2	Surface Modes in Nonspherical Particles	342
12.3	Vibrational Modes in Insulators	357
12.4	Electronic Modes in Metals	369
	Notes and Comments	380

Chapter 13. Angular Dependence of Scattering, 381

13.1 Scattering of Unpolarized and Linearly Polarized Light 381
13.2 Techniques of Measurement and Particle Production 389
13.3 Measurements on Single Particles 394
13.4 Some Theoretical and Experimental Results 397
13.5 Particle Sizing 403
13.6 Scattering Matrix Symmetry 406
13.7 Measurement Techniques for the Scattering Matrix 414
13.8 Some Results for the Scattering Matrix 419
13.9 Summary: Applicability of Mie Theory 427
Notes and Comments 428

Chapter 14. A Miscellany of Applications, 429

14.1 The Problem of Optical Constants 430
14.2 Atmospheric Aerosols 434
14.3 Noctilucent Clouds 448
14.4 Rainfall Measurements with Radar 454
14.5 Interstellar Dust 457
14.6 Pressure Dependence of Intrinsic Optical Spectra Using Small Particles 468
14.7 Giaever Immunological Slide 469
14.8 Microwave Absorption by Macromolecules 472

APPENDIXES COMPUTER PROGRAMS

Appendix A. Homogeneous Sphere, 477

Appendix B. Coated Sphere, 483

Appendix C. Normally Illuminated Infinite Cylinder, 491

References, 499

Index, 521