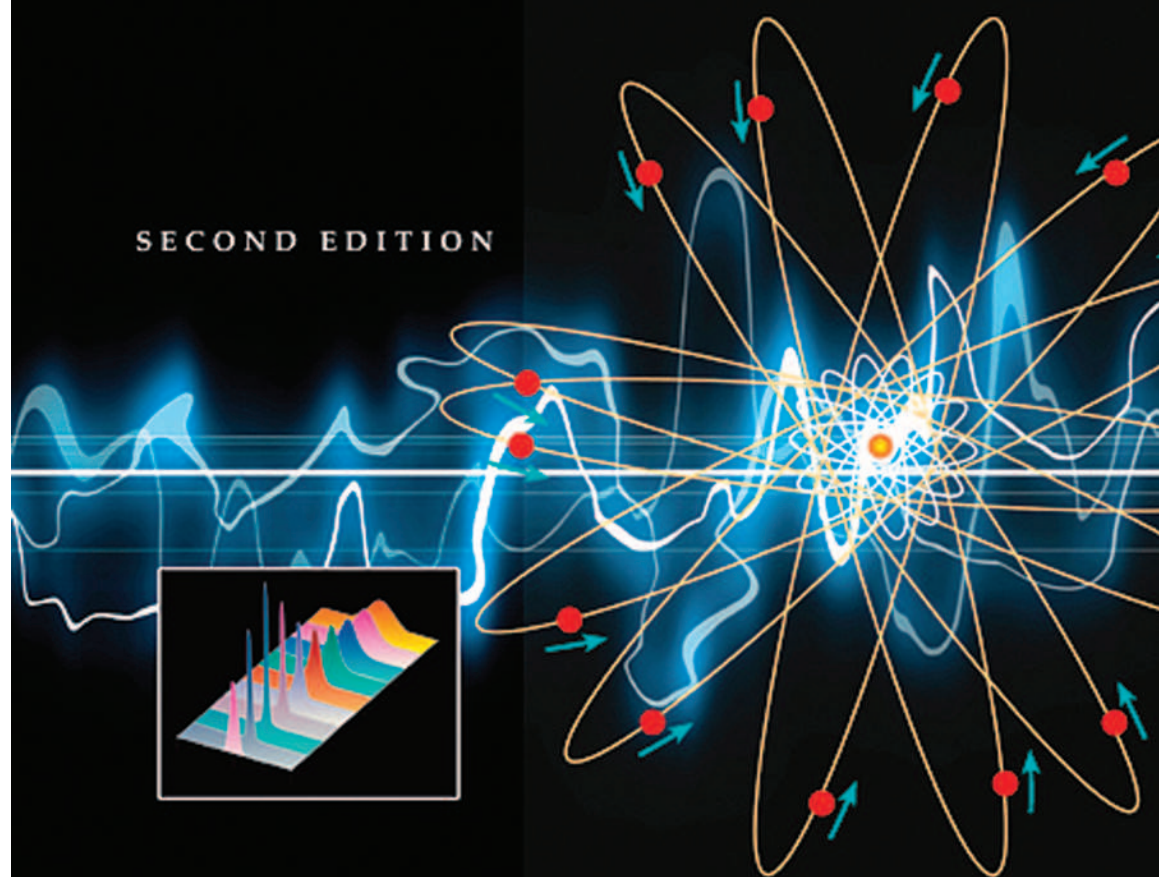


Ultrashort Laser Pulse Phenomena

*Fundamentals, Techniques,
and Applications on a
Femtosecond Time Scale*

SECOND EDITION



Jean-Claude Diels
Wolfgang Rudolph

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Second Edition

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Academic Press is an imprint of Elsevier



Academic Press is an imprint of Elsevier
30 Corporate Drive, Suite 400, Burlington, MA 01803, USA
525 B Street, Suite 1900, San Diego, California 92101-4495, USA
84 Theobald's Road, London WC1X 8RR, UK

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Library of Congress Cataloging-in-Publication Data

Application submitted

British Library Cataloguing-in-Publication Data

A catalogue record for this book is available from the British Library.

ISBN 13: 978-0-12-215493-5

ISBN 10: 0-12-215493-2

For information on all Academic Press publications
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Printed in the United States of America
06 07 08 09 10 9 8 7 6 5 4 3 2 1

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